

NCERT Solutions for Class-XII Maths

Chapter-4.3

NCERT Math Class 12

1. Find area of the triangle with vertices at the point given in each of the following:

(i) (1,0), (6,0),(4,3)

(ii) (2,7),(1,1),(10,8)

(iii) (-2,-3), (3,2),(-1,-8)

1. Area of triangle = $\frac{1}{2} \begin{vmatrix} x_1 & y_1 & 1 \\ x_2 & y_2 & 1 \\ x_3 & y_3 & 1 \end{vmatrix}$

(i) A(1,0), B(6,0), C(4,3)

Area of triangle ABC = $\frac{1}{2} \begin{vmatrix} 1 & 0 & 1 \\ 6 & 0 & 1 \\ 4 & 3 & 1 \end{vmatrix}$

= $\frac{1}{2} [1(0 - 3) - 0(6 - 4) + 1(18 - 0)] = \frac{1}{2} (15) = 7.5$ square units

(ii) A(2,7), B(1,1), C(10,8)

Area of triangle ABC = $\frac{1}{2} \begin{vmatrix} 2 & 7 & 1 \\ 1 & 1 & 1 \\ 10 & 8 & 1 \end{vmatrix}$

= $\frac{1}{2} [2(1 - 8) - 7(1 - 10) + 1(8 - 10)] = \frac{1}{2} (47) = 23.5$ square units

(iii) (-2,-3), (3,2),(-1,-8)

Area of triangle ABC = $\frac{1}{2} \begin{vmatrix} -2 & -3 & 1 \\ 3 & 2 & 1 \\ -1 & -8 & 1 \end{vmatrix}$

= $\frac{1}{2} [-2(2 + 8) + 3(3 + 1) + 1(-24 + 2)] = \frac{1}{2} (-30) = -15$

Area of triangle ABC = 15 square units

2. Show that points A(a, b + c), B(b, c + a), C (c, a + b) are collinear.

2. Given vertices of the triangle are A (a, b + c), B (b, c + a), C (c, a + b)

Let the vertices of the triangle be given by $(x_1, y_1), (x_2, y_2), (x_3, y_3)$

$$\text{Area of triangle is given by } \Delta = \frac{1}{2} \begin{vmatrix} x_1 & y_1 & 1 \\ x_2 & y_2 & 1 \\ x_3 & y_3 & 1 \end{vmatrix}$$

For points to be collinear area of triangle = $\Delta = 0$

So, we have to show that area of triangle formed by ABC is 0

$$\text{Area of triangle} = \Delta = \frac{1}{2} \begin{vmatrix} a & b+c & 1 \\ b & c+a & 1 \\ c & a+b & 1 \end{vmatrix}$$

Expanding the determinant along Row 1

$$\Delta = \frac{1}{2} \times [a \times \{(c+a) \times 1 - (a+b) \times 1\} - (b+c) \times \{b \times 1 - c \times 1\} + 1 \times \{b \times (a+b) - c \times (c+a)\}]$$

$$\Delta = \frac{1}{2} \times [a \times (c+a-a-b) - (b+c) \times (b-c) + 1 \times (ab+b^2-c^2-ca)]$$

$$\Delta = \frac{1}{2} \times [a \times (c-b) - (b^2-c^2) + 1 \times (ab+b^2-c^2-ca)]$$

$$\Delta = \frac{1}{2} \times (ac-ab-b^2+c^2+ab+b^2-c^2-ca) \text{ sq units}$$

$$\Delta = \frac{1}{2} \times 0 \text{ sq units}$$

$$\therefore \Delta = 0$$

\therefore Given vertices of the triangle are A $(a, b+c)$, B $(b, c+a)$, C $(c, a+b)$ are collinear

3. Find value of k if area of triangle is 4 sq. units and vertices are

(i) $(k, 0), (4, 0), (0, 2)$

(ii) $(-2, 0), (0, 4), (0, k)$

3. (i) A $(k, 0)$, B $(4, 0)$, C $(0, 2)$

$$\text{Area of triangle} = \frac{1}{2} \begin{vmatrix} k & 0 & 1 \\ 4 & 0 & 1 \\ 0 & 2 & 1 \end{vmatrix}$$

$$= \frac{1}{2} [k(0-2) - 0(4-0) + 1(8-0)] = \frac{1}{2} (-2k+8) = -k+4$$

According to question, area of triangle $ABC = 4$ square units

$$\text{Therefore, } |-k+4| = 4 \Rightarrow -k+4 = \pm 4$$

$$\Rightarrow -k+4 = 4 \quad \text{or} \quad -k+4 = -4$$

$$\Rightarrow k = 0 \quad \text{or} \quad k = 8$$

Hence, the value of k are 0 and 8

(i) A $(-2, 0)$, B $(0, 4)$, C $(0, k)$

$$\text{Area of triangle } ABC = \frac{1}{2} \begin{vmatrix} -2 & 0 & 1 \\ 0 & 4 & 1 \\ 0 & 5 & 1 \end{vmatrix}$$

$$= \frac{1}{2} [-2(4 - k) - 0(0 - 0) + 1(0 - 0)] = \frac{1}{2} (-8 + 2k) = -4 + k$$

According to question, area of triangle ABC = 4 square units

$$\text{Therefore, } |-4 + k| = 4 \quad \Rightarrow -4 + k = \pm 4$$

$$\Rightarrow -4 + k = 4 \quad \text{or} \quad -4 + k = -4$$

$$\Rightarrow k = 8 \quad \text{or} \quad k = 0$$

Hence, the value of k are 0 and 8.

4. (i) Find equation of line joining (1, 2) and (3, 6) using determinants.
 (ii) Find equation of line joining (3, 1) and (9, 3) using determinants.
 4. (i)

$$\text{Equation of line joining points } (x_1, y_1) \text{ \& } (x_2, y_2) \text{ is given by } \frac{1}{2} \begin{vmatrix} x_1 & y_1 & 1 \\ x_2 & y_2 & 1 \\ x & y & 1 \end{vmatrix} = 0$$

Given points are (1, 2) and (3, 6)

$$\text{Equation of line is given by } \frac{1}{2} \begin{vmatrix} 1 & 2 & 1 \\ 3 & 6 & 1 \\ x & y & 1 \end{vmatrix} = 0$$

$$\Rightarrow \frac{1}{2} \times [1 \times (6 \times 1 - y \times 1) - 2 \times (3 \times 1 - x \times 1) + 1 \times (3 \times y - x \times 6)] = 0$$

$$\Rightarrow [(6 - y) - 2 \times (3 - x) + (3y - 6x)] = 0 \times 2$$

$$\Rightarrow (6 - y - 6 + 2x + 3y - 6x) = 0$$

$$\Rightarrow 2y - 4x = 0$$

$$\Rightarrow y - 2x = 0 \quad \Rightarrow y = 2x$$

∴ Required Equation of line is $y = 2x$

(ii)

$$\text{Equation of line joining points } (x_1, y_1) \text{ \& } (x_2, y_2) \text{ is given by } \frac{1}{2} \begin{vmatrix} x_1 & y_1 & 1 \\ x_2 & y_2 & 1 \\ x & y & 1 \end{vmatrix} = 0$$

Given points are (3, 1) and (9, 3)

Equation of line is given by $\frac{1}{2} \begin{vmatrix} 3 & 1 & 1 \\ 9 & 3 & 1 \\ x & y & 1 \end{vmatrix} = 0$

$$\Rightarrow \frac{1}{2} \times [3 \times (3 \times 1 - y \times 1) - 1 \times (9 \times 1 - x \times 1) + 1 \times (9 \times y - x \times 3)] = 0$$

$$\Rightarrow [3 \times (3 - y) - 1 \times (9 - x) + (9y - 3x)] = 0 \times 2$$

$$\Rightarrow (9 - 3y - 9 + x + 9y - 3x) = 0$$

$$\Rightarrow 6y - 2x = 0$$

$$\Rightarrow 2x - 6y = 0 \Rightarrow x - 3y = 0$$

∴ Required Equation of line is $x - 3y = 0$

5. If area of triangle is 35 sq. units with vertices (2, -6), (5, 4) and (k, 4). Then k is
- (a) 12
 (b) -2
 (c) -12, -2
 (d) 12, -2

5. A(2, -6), B(5,4), C(k, 4)

$$\begin{aligned} \text{Area of triangle } ABC &= \frac{1}{2} \begin{vmatrix} 2 & -6 & 1 \\ 5 & 4 & 1 \\ k & 4 & 1 \end{vmatrix} \\ &= \frac{1}{2} [2(4 - 4) + 6(5 - k) + 1(20 - 4k)] = \frac{1}{2} (30 - 6k + 20 - 4k) = 25 - 5k \end{aligned}$$

According to questions, area of triangle ABC = 35 square units

Therefore, $|25 - 5k| = 35$

$$\Rightarrow 25 - 5k = \pm 35$$

$$\Rightarrow 25 - 5k = 35 \quad \text{or} \quad 25 - 5k = -35$$

$$\Rightarrow k = \frac{-10}{5} = -2 \quad \text{or} \quad k = \frac{60}{5} = 12$$

Hence, the option (d) is correct.