

NCERT Solutions for Class-XII Maths

Chapter-1 Exercise- 1.1

NCERT Math Class 12

1. Determine whether each of the following relations are reflexive, symmetric and transitive:

(i) Relation R in the set $A = \{1, 2, 3 \dots 13, 14\}$ defined as
 $R = \{(x, y) : 3x - y = 0\}$

(ii) Relation R in the set N of natural numbers defined as
 $R = \{(x, y) : y = x + 5 \text{ and } x < 4\}$

(iii) Relation R in the set $A = \{1, 2, 3, 4, 5, 6\}$ as
 $R = \{(x, y) : y \text{ is divisible by } x\}$

(iv) Relation R in the set Z of all integers defined as
 $R = \{(x, y) : x - y \text{ is an integer}\}$

(v) Relation R in the set A of human beings in a town at a particular time given by

(a) $R = \{(x, y) : x \text{ and } y \text{ work at the same place}\}$

(b) $R = \{(x, y) : x \text{ and } y \text{ live in the same locality}\}$

(c) $R = \{(x, y) : x \text{ is exactly } 7 \text{ cm taller than } y\}$

(d) $R = \{(x, y) : x \text{ is wife of } y\}$

(e) $R = \{(x, y) : x \text{ is father of } y\}$

1. (i) $A = \{1, 2, 3 \dots 13, 14\}$

$R = \{(x, y) : 3x - y = 0\}$

$\therefore R = \{(1, 3), (2, 6), (3, 9), (4, 12)\}$

R is not reflexive since $(1, 1), (2, 2) \dots (14, 14) \notin R$.

Also, R is not symmetric as $(1, 3) \in R$, but $(3, 1) \notin R$. [$3(3) - 1 \neq 0$]

Also, R is not transitive as $(1, 3), (3, 9) \in R$, but $(1, 9) \notin R$. [$3(1) - 9 \neq 0$]

Hence, R is neither reflexive, nor symmetric, nor transitive.

(ii) $R = \{(x, y) : y = x + 5 \text{ and } x < 4\} = \{(1, 6), (2, 7), (3, 8)\}$

It is clear that $(1, 1) \notin R$.

$\therefore R$ is not reflexive.

$(1, 6) \in R$ But, $(1, 6) \notin R$.

$\therefore R$ is not symmetric.

Now, since there is no pair in R such that (x, y) and $(y, z) \in R$, then (x, z) cannot belong to R .

$\therefore R$ is not transitive.

Hence, R is neither reflexive, nor symmetric, nor transitive.

(iii) $A = \{1, 2, 3, 4, 5, 6\}$

$R = \{(x, y): y \text{ is divisible by } x\}$

We know that any number (x) is divisible by itself.

So, $(x, x) \in R$

$\therefore R$ is reflexive.

Now,

$(2, 4) \in R$ [as 4 is divisible by 2]

But, $(4, 2) \notin R$. [as 2 is not divisible by 4]

$\therefore R$ is not symmetric.

Let $(x, y), (y, z) \in R$. Then, y is divisible by x and z is divisible by y .

$\therefore z$ is divisible by x .

$\Rightarrow (x, z) \in R$

$\therefore R$ is transitive.

Hence, R is reflexive and transitive but not symmetric.

(iv) $R = \{(x, y): x - y \text{ is an integer}\}$

Now, for every $x \in \mathbb{Z}$, $(x, x) \in R$ as $x - x = 0$ is an integer.

$\therefore R$ is reflexive.

Now, for every $x, y \in \mathbb{Z}$, if $(x, y) \in R$, then $x - y$ is an integer.

$\Rightarrow -(x - y)$ is also an integer.

$\Rightarrow (y - x)$ is an integer.

$\therefore (y, x) \in R$

$\therefore R$ is symmetric.

Now,

Let (x, y) and $(y, z) \in R$, where $x, y, z \in \mathbb{Z}$.

$\Rightarrow (x - y)$ and $(y - z)$ are integers.

$\Rightarrow x - z = (x - y) + (y - z)$ is an integer.

$\therefore (x, z) \in R$

$\therefore R$ is transitive.

Hence, R is reflexive, symmetric, and transitive.

(v)

(a) $R = \{(x, y): x \text{ and } y \text{ work at the same place}\}$

$\Rightarrow (x, x) \in R$ [as x and x work at the same place]

$\therefore R$ is reflexive.

If $(x, y) \in R$, then x and y work at the same place.

$\Rightarrow y$ and x work at the same place.

$\Rightarrow (y, x) \in R$.

$\therefore R$ is symmetric.

Now, let $(x, y), (y, z) \in R$

$\Rightarrow x$ and y work at the same place and y and z work at the same place.

$\Rightarrow x$ and z work at the same place.

$\Rightarrow (x, z) \in R$

$\therefore R$ is transitive.

Hence, R is reflexive, symmetric and transitive.

(b) $R = \{(x, y): x \text{ and } y \text{ live in the same locality}\}$ Clearly, $(x, x) \in R$ as x and x is the same human being. $\therefore R$ is reflexive.

If $(x, y) \in R$, then x and y live in the same locality.

$\Rightarrow y$ and x live in the same locality.

$\Rightarrow (y, x) \in R$

$\therefore R$ is symmetric.

Now, let $(x, y) \in R$ and $(y, z) \in R$.

$\Rightarrow x$ and y live in the same locality and y and z live in the same locality.

$\Rightarrow x$ and z live in the same locality.

$\Rightarrow (x, z) \in R$

$\therefore R$ is transitive.

Hence, R is reflexive, symmetric and transitive.

(c) $R = \{(x, y): x \text{ is exactly } 7 \text{ cm taller than } y\}$ Now, $(x, x) \notin R$

Since human being x cannot be taller than himself. $\therefore R$ is not reflexive.

Now, let $(x, y) \in R$.

$\Rightarrow x$ is exactly 7 cm taller than y .

Then, y is not taller than x . [Since, y is 7 cm smaller than x]

$\therefore (y, x) \notin R$

Indeed if x is exactly 7 cm taller than y , then y is exactly 7 cm shorter than x . $\therefore R$ is not symmetric.

Now,

Let $(x, y), (y, z) \in R$.

$\Rightarrow x$ is exactly 7 cm taller than y and y is exactly 7 cm taller than z .

$\Rightarrow x$ is exactly 14 cm taller than z .

$\therefore (x, z) \notin R$

$\therefore R$ is not transitive.

Hence, R is neither reflexive, nor symmetric, nor transitive.

(d) $R = \{(x, y): x \text{ is the wife of } y\}$

Now,

$(x, x) \notin R$

Since x cannot be the wife of herself.

$\therefore R$ is not reflexive.

Now, let $(x, y) \in R$

$\Rightarrow x$ is the wife of y .

Clearly y is not the wife of x .

$\therefore (y, x) \notin R$

Indeed if x is the wife of y , then y is the husband of x . $\therefore R$ is not transitive.

Let $(x, y), (y, z) \in R$

$\Rightarrow x$ is the wife of y and y is the wife of z .

This case is not possible. Also, this does not imply that x is the wife of z . $\therefore (x, z) \notin R$

$\therefore R$ is not transitive.

Hence, R is neither reflexive, nor symmetric, nor transitive.

(e) $R = \{(x, y) : x \text{ is the father of } y\}$

$(x, x) \notin R$

As x cannot be the father of himself.

$\therefore R$ is not reflexive.

Now, let $(x, y) \in R$.

$\Rightarrow x$ is the father of y .

$\Rightarrow y$ cannot be the father of y .

Indeed, y is the son or the daughter of y . $\therefore (y, x) \notin R$

$\therefore R$ is not symmetric.

Now, let $(x, y) \in R$ and $(y, z) \notin R$.

$\Rightarrow x$ is the father of y and y is the father of z .

$\Rightarrow x$ is not the father of z .

Indeed, x is the grandfather of z .

$\therefore (x, z) \notin R$

$\therefore R$ is not transitive.

Hence, R is neither reflexive, nor symmetric, nor transitive.

2. Show that the relation R in the set R of real numbers, defined as $R = \{(a, b) : a \leq b^2\}$ is neither reflexive nor symmetric nor transitive.
2. It is given that $R = \{(a, b) : a \leq b^2\}$

We can see that $\left(\frac{1}{2}, \frac{1}{2}\right) \notin R$,

Since, $\frac{1}{2} > \left(\frac{1}{2}\right)^2$

Therefore, R is not reflexive.

Now, $(1, 4) \in R$ as $1 < 4^2$

But 4 is not less than 1^2 .

Then, $(4,1) \notin R$

Therefore, R is not symmetric.

Now, $(3,2), (2,1.5) \in R$

But, $3 > (1.5)^2 = 2.25$.

Then, $(3, 1.5) \notin R$

Therefore, R is not transitive.

Therefore, R is neither reflexive, nor symmetric, nor transitive.

3. Check whether the relation R defined in the set $\{1, 2, 3, 4, 5, 6\}$ as $R = \{(a, b): b = a + 1\}$ is reflexive, symmetric or transitive.

3. Let $A = \{1, 2, 3, 4, 5, 6\}$.

A relation R is defined on set A as: $R = \{(a, b): b = a + 1\}$

$\therefore R = \{(1, 2), (2, 3), (3, 4), (4, 5), (5, 6)\}$

we can find $(a, a) \notin R$, where $a \in A$.

For instance,

$(1, 1), (2, 2), (3, 3), (4, 4), (5, 5), (6, 6) \notin R$

$\therefore R$ is not reflexive.

It can be observed that $(1, 2) \in R$, but $(2, 1) \notin R$.

$\therefore R$ is not symmetric.

Now, $(1, 2), (2, 3) \in R$

But, $(1, 3) \notin R$

$\therefore R$ is not transitive

Hence, R is neither reflexive, nor symmetric, nor transitive.

4. Show that the relation R in R defined as $R = \{(a, b): a \leq b\}$, is reflexive and transitive but not symmetric.

4. It is given that $R = \{(a, b): a \leq b\}$,

It is clear that $(a,a) \in R$ as $a = a$.

Therefore, R is reflexive.

Now let us take $(2,4) \in R$ ($2 < 4$)

But, $(4,2) \notin R$ as 4 is greater than 2.

Therefore, R is not symmetric.

Now, let $(a,b), (b,c) \in R$

Then, $a \leq b$ and $b \leq c$

$\Rightarrow a \leq c$

$\Rightarrow (a,c) \in R$

Therefore, R is a transitive.

Therefore, R is reflexive and transitive but not symmetric.

5. Check whether the relation R in R defined as $R = \{(a, b): a \leq b^3\}$ is reflexive, symmetric or transitive.

5. $R = \{(a, b): a \leq b^3\}$

It is observed that $\left(\frac{1}{2}, \frac{1}{2}\right) \notin R$, since, $\frac{1}{2} > \left(\frac{1}{2}\right)^3$

$\therefore R$ is not reflexive.

Now, $(1, 2) \in R$ (as $1 < 2^3 = 8$)

But, $(2, 1) \notin R$ (as $2^3 > 1$)

$\therefore R$ is not symmetric.

We have $\left(3, \frac{3}{2}\right), \left(\frac{3}{2}, \frac{6}{5}\right) \in R$, since $3 < \left(\frac{3}{2}\right)^3$ and $\frac{3}{2} < \left(\frac{6}{5}\right)^3$

But $\left(3, \frac{6}{5}\right) \notin R$ as $3 > \left(\frac{6}{5}\right)^3$

$\therefore R$ is not transitive.

Hence, R is neither reflexive, nor symmetric, nor transitive.

6. Show that the relation R in the set $\{1, 2, 3\}$ given by $R = \{(1, 2), (2, 1)\}$ is symmetric but neither reflexive nor transitive.

6. Let us take $A = \{1, 2, 3\}$

A relation R is defined on set A as $R = \{(1,2), (2,1)\}$

It is seen that $(1,1), (2,2), (3,3) \notin R$.

Therefore, R is not reflexive.

Now, we can see that $(1,2) \in R$ and $(2,1) \in R$

Therefore, R is symmetric.

And now, $(1,2), (2,1) \in R$

But, $(1,1) \notin R$

Therefore, R is not transitive.

Therefore, R is symmetric but neither reflexive, nor transitive.

7. Show that the relation R in the set A of all the books in a library of a college, given by $R = \{(x, y): x \text{ and } y \text{ have same number of pages}\}$ is an equivalence relation.

7. Set A is the set of all books in the library of a college.

$R = \{(x, y): x \text{ and } y \text{ have the same number of pages}\}$

Now, R is reflexive since $(x, x) \in R$ as x and x has the same number of pages. Let $(x, y) \in R \Rightarrow x$ and y have the same number of pages.

$\Rightarrow y$ and x have the same number of pages.

$\Rightarrow (y, x) \in R$

$\therefore R$ is symmetric.

Now, let $(x, y) \in R$ and $(y, z) \in R$.

$\Rightarrow x$ and y have the same number of pages and y and z have the same number of pages.

$\Rightarrow x$ and z have the same number of pages.

$\Rightarrow (x, z) \in R$

$\therefore R$ is transitive.

Hence, R is an equivalence relation.

8. Show that the relation R in the set $A = \{1, 2, 3, 4, 5\}$ given by $R = \{(a, b) : |a - b| \text{ is even}\}$, is an equivalence relation. Show that all the elements of $\{1, 3, 5\}$ are related to each other and all the elements of $\{2, 4\}$ are related to each other. But no element of $\{1, 3, 5\}$ is related to any element of $\{2, 4\}$.

8. It is given that the relation R in the set $A = \{1, 2, 3, 4, 5\}$

given by $R = \{(a, b) : |a - b| \text{ is even}\}$,

It is clear that for any element $a \in A$, we have $|a - a| = 0$ (which is even)

Therefore, R is reflexive.

Now, Let $(a, b) \in R$

$\Rightarrow |a - b|$ is even

$\Rightarrow |-(a - b)| = |b - a|$ is also even.

$\Rightarrow (b, a) \in R$

Therefore, R is symmetric.

Now, Let $(a, b) \in R$ and $(b, c) \in R$.

$\Rightarrow |a - b|$ is even and $|b - c|$ is even

$\Rightarrow (a - b)$ is even and $(b - c)$ is even

$\Rightarrow (a - c) = (a - b) + (b - c)$ is even

$\Rightarrow |a - c|$ is even

$\Rightarrow (a, c) \in R$

Therefore, R is transitive.

Therefore, R is an equivalence relation.

Now, all elements of the set $\{1, 3, 5\}$ are related to each other as all the elements of this subset are odd.

Therefore, the modulus of the difference between any two elements will be even.

Similarly, all elements of the sets $\{2, 4\}$ are related each other as all the elements of this subset are even.

Also, no element of the subset $\{1, 3, 5\}$ can be related to any element of $\{2, 4\}$ as all elements of $\{1, 3, 5\}$ are odd and all elements of $\{2, 4\}$ are even.

Therefore, the modulus of the difference between the two elements will not be even.

9. Show that each of the relation R in the set $A = \{x \in \mathbf{Z}: 0 \leq x \leq 12\}$, given by

(i) $R = \{(a, b) : |a - b| \text{ is a multiple of } 4\}$

(ii) $R = \{(a, b) : a = b\}$

is an equivalence relation. Find the set of all elements related to 1 in each case.

9. $A = \{x \in \mathbf{Z}: 0 \leq x \leq 12\} = \{0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12\}$

(i) $R = \{(a, b) : |a - b| \text{ is a multiple of } 4\}$

For any element $a \in A$, we have $(a, a) \in R$ as $|a - a| = 0$ is a multiple of 4. $\therefore R$ is reflexive.

Now, let $(a, b) \in R \Rightarrow |a - b|$ is a multiple of 4.

$\Rightarrow |-(a - b)| = |b - a|$ is a multiple of 4.

$\Rightarrow (b, a) \in R$

$\therefore R$ is symmetric.

Now, let $(a, b), (b, c) \in R$.

$\Rightarrow |a - b|$ is a multiple of 4 and $|b - c|$ is a multiple of 4.

$\Rightarrow (a - b)$ is a multiple of 4 and $(b - c)$ is a multiple of 4.

$\Rightarrow (a - c) = (a - b) + (b - c)$ is a multiple of 4.

$\Rightarrow |a - c|$ is a multiple of 4.

$\Rightarrow (a, c) \in R$

$\therefore R$ is transitive.

Hence, R is an equivalence relation.

The set of elements related to 1 is $\{1, 5, 9\}$ as

$|1 - 1| = 0$ is a multiple of 4.

$|5 - 1| = 4$ is a multiple of 4.

$|9 - 1| = 8$ is a multiple of 4.

(ii) $R = \{(a, b) : a = b\}$

For any element $a \in A$, we have $(a, a) \in R$, since $a = a$.

$\therefore R$ is reflexive.

Now, let $(a, b) \in R$.

$\Rightarrow a = b$

$\Rightarrow b = a \Rightarrow (b, a) \in R$

$\therefore R$ is symmetric.

Now, let $(a, b) \in R$ and $(b, c) \in R$.

$\Rightarrow a = b$ and $b = c$

$\Rightarrow a = c$

$\Rightarrow (a, c) \in R$

$\therefore R$ is transitive.

Hence, R is an equivalence relation.

The elements in R that are related to 1 will be those elements from set A which are equal to 1.

Hence, the set of elements related to 1 is $\{1\}$.

10. Given an example of a relation. Which is
- (i) Symmetric but neither reflexive nor transitive.
 - (ii) Transitive but neither reflexive nor symmetric.
 - (iii) Reflexive and symmetric but not transitive.
 - (iv) Reflexive and transitive but not symmetric.
 - (v) Symmetric and transitive but not reflexive.

10. (i) Let $A = \{3,4,5\}$

Define a relation R on A as $R = \{(3,4), (4,3)\}$

Relation R is not reflexive as $(3,3), (4,4)$ and $(5,5) \notin R$.

Now, as $(3,4) \in R$ and also $(4,3) \in R$,

R is symmetric.

$\Rightarrow (3,4), (4,3) \in R$, but $(3,3) \notin R$

$\Rightarrow R$ is not transitive.

Therefore, relation R is symmetric but not reflexive or transitive.

- (ii) Let a relation R in R defined as:

$$R = \{(a,b) : a < b\}$$

For any $a \in R$, we have $(a,a) \notin R$ as a cannot be strictly less than a itself.

In fact, $a = a$,

Therefore, R is not reflexive.

Now, $(1,2) \in R$ but $2 > 1$

$\Rightarrow (2,1) \notin R$.

$\Rightarrow R$ is not symmetric.

Now, let $(a,b), (b,c) \in R$

$\Rightarrow a < b$ and $b < c$

$\Rightarrow a < c$

$\Rightarrow (a,c) \in R$

$\Rightarrow R$ is transitive.

Therefore, relation R is transitive but not reflexive and a symmetric.

- (iii) Let us take $A = \{2,4,6\}$

Define a relation R on A as:

$$A = \{(2,2), (4,4), (6,6), (2,4), (4,2), (4,6), (6,4)\}$$

Relation of R is reflexive as for every $a \in A$,

$(a,a) \in R$

$\Rightarrow (2,2), (4,4), (6,6) \in R$,

Relation R is symmetric as $(a,b) \in R$

$\Rightarrow (b,a) \in R$ for all $a, b \in R$

And Relation R is not transitive as $(2,4), (4,6) \in R$,
but $(2,6) \notin R$

Therefore, relation R is reflexive and symmetric but not transitive.

(iv) Let us define a relation R in R as

$$R = \{(a,b) : a^3 \geq b^3\}$$

It is clear that $(a,a) \in R$ as $a^3 = a^3$

\Rightarrow R is reflexive.

Now, $(2,1) \in R$

But $(1,2) \notin R$

\Rightarrow R is not symmetric.

Now, let $(a,b), (b,c) \in R$

$\Rightarrow a^3 \geq b^3$ and $b^3 \geq c^3$

$\Rightarrow a^3 \geq c^3$

$\Rightarrow (a,c) \in R$

\Rightarrow R is transitive.

Therefore, relation R is reflexive and transitive but not symmetric.

(v) Let $A = \{-7,-8\}$

Define a relation R on A as:

$$R = \{(-7,-8), (-8,-7), (-7,-7)\}$$

Relation R is not reflexive as $(-8,-8) \notin R$

Relation R is symmetric as $(-7,-8) \in R$ and $(-8,-7) \in R$

But it is seen that $(-7,-8), (-8,-7) \in R$.

Also, $(-7,-7) \in R$.

\Rightarrow R is transitive.

Therefore, relation R is symmetric and transitive but not reflexive.

11. Show that the relation R in the set A of points in a plane given by $R = \{(P, Q) : \text{Distance of the point P from the origin is same as the distance of the point Q from the origin}\}$, is an equivalence relation. Further, show that the set of all point related to a point $P \neq (0, 0)$ is the circle passing through P with origin as centre.

11. $R = \{(P, Q) : \text{Distance of point P from the origin is the same as the distance of point Q from the origin}\}$

Clearly, $(P, P) \in R$ since the distance of point P from the origin is always the same as the distance of the same point P from the origin.

\therefore R is reflexive.

Now, Let $(P, Q) \in R$.

\Rightarrow The distance of point P from the origin is the same as the distance of point Q from the origin.

⇒ The distance of point Q from the origin is the same as the distance of point P from the origin.

⇒ $(Q, P) \in R$

∴ R is symmetric.

Now, Let $(P, Q), (Q, S) \in R$.

⇒ The distance of points P and Q from the origin is the same and also, the distance of points Q and S from the origin is the same.

⇒ The distance of points P and S from the origin is the same.

⇒ $(P, S) \in R$

∴ R is transitive.

Therefore, R is an equivalence relation.

The set of all points related to $P \neq (0, 0)$ will be those points whose distance from the origin is the same as the distance of point P from the origin.

In other words, if O (0, 0) is the origin and $OP = k$, then the set of all points related to P is at a distance of k from the origin.

Hence, this set of points forms a circle with the centre as the origin and this circle passes through point P.

11. Show that the relation R defined in the set A of all triangles as $R = \{(T_1, T_2): T_1 \text{ is similar to } T_2\}$, is equivalence relation. Consider three right angle triangles T_1 with sides 3, 4, 5, T_2 with sides 5, 12, 13 and T_3 with sides 6, 8, 10. Which triangles among T_1, T_2 and T_3 are related?

12. It is given that the relation R defined in the set A of all triangles as

$R = \{(T_1, T_2): T_1 \text{ is similar to } T_2\}$,

Now, R is reflexive as every triangle is similar to itself.

Now, if $(T_1, T_2) \in R$, then T_1 is similar to T_2 .

⇒ T_2 is similar to T_1 .

⇒ $(T_1, T_2) \in R$

Therefore, R is symmetric.

Now, if $(T_1, T_2), (T_2, T_3) \in R$,

⇒ T_1 is similar to T_2 and T_2 is similar to T_3 .

⇒ T_1 is similar to T_3 .

⇒ $(T_1, T_3) \in R$

Therefore, R is transitive.

Therefore, R is equivalence relation.

Now, we can see that,

$$\frac{3}{6} = \frac{4}{8} = \frac{5}{10} = \frac{1}{2}$$

Therefore, the corresponding sides of triangles T_1 and T_3 are in the same ratio.

Thus, triangle T_1 is similar to triangle T_3 .

Therefore, T_1 is related to T_3 .

- 13.** Show that the relation R defined in the set A of all polygons as $R = \{(P_1, P_2): P_1 \text{ and } P_2 \text{ have same number of sides}\}$, is an equivalence relation. What is the set of all elements in A related to the right-angle triangle T with sides 3, 4 and 5?

- 13.** $R = \{(P_1, P_2): P_1 \text{ and } P_2 \text{ have same the number of sides}\}$

R is reflexive,

Since $(P_1, P_1) \in R$, as the same polygon has the same number of sides with itself.

Let $(P_1, P_2) \in R$.

$\Rightarrow P_1$ and P_2 have the same number of sides.

$\Rightarrow P_2$ and P_1 have the same number of sides.

$\Rightarrow (P_2, P_1) \in R$

$\therefore R$ is symmetric.

Now,

Let $(P_1, P_2), (P_2, P_3) \in R$.

$\Rightarrow P_1$ and P_2 have the same number of sides.

Also, P_2 and P_3 have the same number of sides.

$\Rightarrow P_1$ and P_3 have the same number of sides.

$\Rightarrow (P_1, P_3) \in R$

$\therefore R$ is transitive.

Hence, R is an equivalence relation.

The elements in A related to the right-angled triangle (T) with sides 3, 4, and 5 are those polygons which have 3 sides (Since T is a polygon with 3 sides). Hence, the set of all elements in A related to triangle T is the set of all triangles.

- 14.** Let L be the set of all lines in XY plane and R be the relation in L defined as $R = \{(L_1, L_2): L_1 \text{ is parallel to } L_2\}$. Show that R is an equivalence relation. Find the set of all lines related to the line $y = 2x + 4$.

- 14.** It is given that the relation in L defined as

$R = \{(L_1, L_2): L_1 \text{ is parallel to } L_2\}$

R is reflexive as any line L_1 is parallel to itself

$\Rightarrow (L_1, L_1) \in R$

Now, Let $(L_1, L_2) \in R$

$\Rightarrow L_1$ is parallel to L_2 .

$\Rightarrow L_2$ is parallel to L_1 .

$\Rightarrow (L_2, L_1) \in R$

Therefore, R is symmetric.

Now, Let $(L_1, L_2), (L_2, L_3) \in R$

$\Rightarrow L_1$ is parallel to L_2 . Also, L_2 is parallel to L_3 .

$\Rightarrow L_1$ is parallel to L_3 .

$\Rightarrow (L_1, L_3) \in R$

Therefore, R is transitive.

Therefore, R is an equivalence relation.

The set of all lines related to the line $y = 2x + 4$ is the set of all lines that are parallel to the line

$$y = 2x + 4$$

Slope of line $y = 2x + 4$ is $m = 2$

We know that parallel lines have the same slopes.

The line parallel to the given line is of the form $y = 2x + c$ where, $c \in R$.

Therefore, the set of all lines related to the given line by $y = 2x + c$, where $c \in R$.

15. Let R be the relation in the set $\{1, 2, 3, 4\}$ given by $R = \{(1, 2), (2, 2), (1, 1), (4, 4), (1, 3), (3, 3), (3, 2)\}$. Choose the correct answer.

(A) R is reflexive and symmetric but not transitive.

(B) R is reflexive and transitive but not symmetric.

(C) R is symmetric and transitive but not reflexive.

(D) R is an equivalence relation.

15. $R = \{(1, 2), (2, 2), (1, 1), (4, 4), (1, 3), (3, 3), (3, 2)\}$

It is seen that $(a, a) \in R$, for every $a \in \{1, 2, 3, 4\}$.

$\therefore R$ is reflexive.

It is seen that $(1, 2) \in R$, but $(2, 1) \notin R$.

$\therefore R$ is not symmetric.

Also, it is observed that $(a, b), (b, c) \in R \Rightarrow (a, c) \in R$ for all $a, b, c \in \{1, 2, 3, 4\}$.

$\therefore R$ is transitive.

Hence, R is reflexive and transitive but not symmetric.

The correct answer is B.

16. Let R be the relation in the set N given by $R = \{(a, b): a = b - 2, b > 6\}$. Choose the correct answer.

(A) $(2, 4) \in R$

(B) $(3, 8) \in R$

(C) $(6, 8) \in R$

(D) $(8, 7) \in R$

16. $R = \{(a, b): a = b - 2, b > 6\}$

Now,

Since $b > 6$, $(2, 4) \notin R$ Also, as $3 \neq 8 - 2$,

$\therefore (3, 8) \notin R$

And, as $8 \neq 7 - 2$

$\therefore (8, 7) \notin R$

Now, consider $(6, 8)$.

We have $8 > 6$ and also, $6 = 8 - 2$.

$\therefore (6, 8) \in R$

The correct answer is C.



Myclass24
Your Class. Your Pace.



Myclass24
Your Class. Your Pace.



Myclass24
Your Class. Your Pace.