

Chapter 2 - Compound Interest

Exercise 2(A)

1. ₹16,000 is invested at 5% compound interest compounded per annum. Use the table, given below, to find the amount in 4 years.

Year	Initial amount (₹)	Interest (₹)	Final amount
1 st	16,000	800	16,800
2 nd			
3 rd			
4 th			
5 th			

Solution:

Year	Initial amount (₹)	Interest (₹)	Final amount
1 st	16,000	800	16,800
2 nd	16,800	840	17,640
3 rd	17,640	882	18,522
4 th	18,522	926.10	19,448.10
5 th	19,448.10	972.405	20,420.505

Thus, the amount in 4 years is ₹19,448.10

2.(i) Calculate the amount and the compound interest on:

₹6000 in 3 years at 5% per year.

(ii) Calculate amount and the compound interest on:

₹8000 in 2½ years at 15% per annum.

Solution:

(i) Given: P = ₹6,000; N = 3 years and R = 5% For

the 1st year

P = ₹6000; N = 1 year and R = 5%

$$\begin{aligned}\text{Interest} &= (6000 \times 5 \times 1)/100 \\ &= ₹300\end{aligned}$$

$$\begin{aligned}\text{And, amount} &= ₹(6000 + 300) \\ &= ₹6,300\end{aligned}$$

For the 2nd year

P = ₹6300; N = 1 year and R = 5%

$$\begin{aligned}\text{Interest} &= (6300 \times 5 \times 1)/100 \\ &= ₹315\end{aligned}$$

$$\begin{aligned}\text{And, amount} &= ₹(6300 + 315) \\ &= ₹6,615\end{aligned}$$

For the 3rd year

P = ₹6,615; N = 1 year and R = 5%

$$\begin{aligned}\text{Interest} &= (6615 \times 5 \times 1)/100 \\ &= ₹330.75\end{aligned}$$

$$\text{And, amount} = ₹(6,615 + 330.75)$$

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$$= ₹6,945.75$$

Hence, the C.I. accrued = Final amount – Initial principal
= ₹6,945.75 - ₹6,000
= ₹945.75

(ii) Given: P = 8000; N = 2½ years and R = 15%

For the 1st year

$$P = ₹8,000; N = 1 \text{ year and } R = 15\%$$

$$\text{Interest} = (8000 \times 15 \times 1)/100 \\ = ₹1,200$$

$$\text{And, amount} = ₹(8,000 + 1,200) \\ = ₹9,200$$

For the 2nd year

$$P = ₹9,200; N = 1 \text{ year and } R = 15\%$$

$$\text{Interest} = (9200 \times 15 \times 1)/100 \\ = ₹1,380$$

$$\text{And, amount} = ₹(9,200 + 1,380) \\ = ₹10,580$$

For the next ½ year

$$P = ₹10,580; N = \frac{1}{2} \text{ year and } R = 15\%$$

$$\text{Interest} = (10580 \times 15 \times \frac{1}{2})/100 \\ = ₹793.50$$

$$\text{And, amount} = ₹(10,580 + 793.50) \\ = ₹11,373.50$$

Hence, the C.I. accrued = Final amount – Initial principal
= ₹11,373.50 - ₹8,000
= ₹3,373.50

3. Calculate the amount and the compound interest on:

(i) ₹4,600 in 2 years when the rates of interest of successive years are 10% and 12% respectively.

(ii) ₹6,000 in 3 years, when the rates of the interest for successive years are 10%, 14% and 15% respectively.

Solution:

(i) For 1st year

$$P = ₹4,600; R = 10\% \text{ and } T = 1 \text{ year}$$

$$= (4600 \times 10 \times 1)/100 \\ = ₹460$$

And,

$$A = ₹(4,600 + 460) \\ = ₹5,060$$

For 2nd year

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Compound Interest (Without Using Formula)**

$$\begin{aligned} P &= ₹5,060; R = 12\% \text{ and } T = 1 \text{ year. } I \\ &= (5060 \times 12 \times 1)/100 \\ &= 60720/100 \\ &= ₹607.20 \end{aligned}$$

And,

$$\begin{aligned} A &= ₹(5,060 + 607.20) \\ &= ₹5,667.20 \end{aligned}$$

$$\begin{aligned} \text{Compound interest} &= ₹(5,667.20 - 4,600) \\ &= ₹1,067.20 \end{aligned}$$

$$\text{Amount after 2 years} = ₹5,667.20$$

(ii) For 1st year

$$\begin{aligned} P &= ₹16,000; R = 10\% \text{ and } T = 1 \text{ year } I \\ &= (16000 \times 10 \times 1)/100 \\ &= ₹1,600 \end{aligned}$$

And,

$$\begin{aligned} A &= ₹(16,000 + 1,600) \\ &= ₹17,600 \end{aligned}$$

For 2nd year

$$\begin{aligned} P &= ₹17,600; R = 14\% \text{ and } T = 1 \text{ year } I \\ &= (17600 \times 14 \times 1)/100 \\ &= 246400/100 \\ &= ₹2,464 \end{aligned}$$

And,

$$\begin{aligned} A &= ₹(17,600 + 2,464) \\ &= ₹20,064 \end{aligned}$$

For 3rd year,

$$\begin{aligned} P &= ₹20,064; R = 15\% \text{ and } T = 1 \text{ year } I \\ &= (20064 \times 15 \times 1)/100 \\ &= ₹3,009.60 \end{aligned}$$

And,

$$\begin{aligned} \text{Amount after 3 years} &= ₹(20,064 + 3,009.60) \\ &= ₹23,073.60 \end{aligned}$$

Hence,

$$\begin{aligned} \text{Compound interest} &= ₹(23,073.60 - 16,000) \\ &= ₹7,073.60 \end{aligned}$$

4. Find the compound interest, correct to the nearest rupee, on ₹2,400 for 2½ years at 5 per cent per annum.

Solution:

For 1st year

$$P = ₹2400; R = 5\% \text{ and } T = 1 \text{ year}$$

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Compound Interest (Without Using Formula)**

$$\begin{aligned}I &= (2400 \times 5 \times 1)/100 \\ &= ₹120 \\ A &= ₹(2400 + 120) \\ &= ₹2520\end{aligned}$$

For 2nd year

$$\begin{aligned}P &= ₹2520; R = 5\% \text{ and } T = 1 \text{ year} \\ I &= (2520 \times 5 \times 1)/100 \\ &= ₹126 \\ A &= ₹(2,520 + 126) \\ &= ₹2,646\end{aligned}$$

For the final $\frac{1}{2}$ year

$$\begin{aligned}P &= \text{Rs. } 2646; R = 5\% \text{ and } T = \frac{1}{2} \text{ year} \\ I &= (2646 \times 5 \times 1)/(100 \times 2) \\ &= ₹66.15 \\ \text{Amount after } 2\frac{1}{2} \text{ years} &= ₹2,646 + ₹66.15 \\ &= ₹2,712.15\end{aligned}$$

Hence,

$$\begin{aligned}\text{Compound interest} &= ₹(2,712.15 - 2,400) \\ &= ₹312.15\end{aligned}$$

5. Calculate the compound interest for the second year on ₹8,000 invested for 3 years at 10% per annum.

Solution:

For 1st year

$$\begin{aligned}P &= ₹8,000; R = 10\% \text{ and } T = 1 \text{ year} \\ I &= (8000 \times 10 \times 1)/100 \\ &= 800\end{aligned}$$

And,

$$A = ₹(8,000 + 800) = ₹8,800$$

For 2nd year

$$\begin{aligned}P &= ₹8,800; R = 10\% \text{ and } T = 1 \text{ year} \\ I &= (8800 \times 10 \times 1)/100 \\ &= ₹880\end{aligned}$$

Hence,

$$\text{Compound interest for } 2^{\text{nd}} \text{ years} = ₹880$$

6. A borrowed ₹2,500 from B at 12% per annum compound interest. After 2 years, A gave ₹2,936 and a watch to B to clear the account. Find the cost of the watch.

Solution:

For 1st year

$$P = ₹2500; R = 12\% \text{ and } T = 1 \text{ year}$$

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$$I = (2500 \times 12 \times 1)/100 \\ = ₹300$$

And,

$$\text{Amount} = ₹(2,500 + 300) = ₹2,800$$

For 2nd year

$$P = ₹2,800; R = 12\% \text{ and } T = 1 \text{ year} \\ I = (2800 \times 12 \times 1)/100 \\ = ₹336$$

And,

$$\text{Amount} = ₹(2,800 + 336) = ₹3136$$

Now,

$$\text{Amount repaid by A to B} = ₹2936$$

$$\text{The amount of watch} = ₹(3136 - 2936) = ₹200$$

7. How much will ₹50,000 amount to in 3 years, compounded yearly, if the rates for the successive years are 6%, 8% and 10% respectively?

Solution:

Given: $P = ₹50,000$; $T = 3$ years

Interest for the 1st year, $R = 6\%$

$$I = (P \times R \times T)/100 \\ = (50000 \times 6 \times 1)/100 \\ = ₹3,000$$

And,

$$\text{Amount after the 1st year} = ₹(3,000 + 50,000) \\ = ₹53,000$$

Now,

Interest for the 2nd year, $R = 8\%$ and $P = ₹53,000$

$$I = (P \times R \times T)/100 \\ = (53000 \times 8 \times 1)/100 \\ = ₹4,240$$

And,

$$\text{Amount after the 2nd year} = ₹(4,240 + 53,000) \\ = ₹57,240$$

Next,

Interest for the 3rd year, $R = 10\%$ and $P = ₹57,240$

$$I = (P \times R \times T)/100 \\ = (57240 \times 10 \times 1)/100 \\ = ₹5,724$$

And,

$$\text{Amount after the 3rd year} = ₹(5,724 + 57,240) \\ = ₹62,964$$

Hence, the amount after 3 years will be ₹62,964

8. Meenal lends ₹75,000 at C.I. for 3 years. If the rate of interest for the first two years is

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15% per year and for the third year it is 16%, calculate the sum Meenal will get at the end of the third year.

Solution:

Given: $P = ₹75,000$; $T = 3$ years

Interest for the 1st year, $R = 15\%$

$$\begin{aligned} I &= (P \times R \times T)/100 \\ &= (75000 \times 15 \times 1)/100 \\ &= ₹11,250 \end{aligned}$$

And,

$$\begin{aligned} \text{Amount after the 1}^{\text{st}} \text{ year} &= ₹(75,000 + 11,250) \\ &= ₹86,250 \end{aligned}$$

Now,

Interest for the 2nd year, $R = 15\%$ and $P = ₹86,250$

$$\begin{aligned} I &= (P \times R \times T)/100 \\ &= (86250 \times 15 \times 1)/100 \\ &= ₹12,937.50 \end{aligned}$$

And,

$$\begin{aligned} \text{Amount after the 2}^{\text{nd}} \text{ year} &= ₹(12,937.50 + 86,250) \\ &= ₹99,187.50 \end{aligned}$$

Next,

Interest for the 3rd year, $R = 16\%$ and $P = ₹99,187.50$

$$\begin{aligned} I &= (P \times R \times T)/100 \\ &= (99187.50 \times 16 \times 1)/100 \\ &= ₹15,870 \end{aligned}$$

And,

$$\begin{aligned} \text{Amount after the 3}^{\text{rd}} \text{ year} &= ₹(15,870 + 99,187.50) \\ &= ₹1,15,057.5 \end{aligned}$$

Hence, at the end of 3 years Meenal will get an amount of ₹1,15,057.5

9. Govind borrows ₹18,000 at 10% simple interest. He immediately invests the money borrowed at 10% compound interest compounded half-yearly. How much money does Govind gain in one year?

Solution:

Calculating the simple interest

$P = ₹18,000$; $R = 10\%$ and $T = 1$ year, we have

$$\begin{aligned} \text{S.I.} &= (18000 \times 10 \times 1)/100 \\ &= ₹1,800 \end{aligned}$$

Calculating the compound interest (compounded half-yearly)

For 1st half- year

$P = ₹18,000$; $R = 10\%$ and $T = \frac{1}{2}$ year

$$\begin{aligned} \text{Interest} &= (18000 \times 10 \times 1)/(100 \times 2) \\ &= ₹900 \end{aligned}$$

So,

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$$\text{Amount} = ₹18,000 + ₹900 = ₹18,900$$

Now,

For 2nd half-year

$$P = ₹18,900; R = 10\% \text{ and } T = \frac{1}{2} \text{ year}$$

$$\begin{aligned} \text{Interest} &= (18,900 \times 10 \times 1)/(100 \times 2) \\ &= ₹945 \text{ Rs} \end{aligned}$$

So,

$$\text{Amount} = ₹18,900 + ₹945 = ₹19,845$$

Then,

$$\text{Compound interest} = ₹(19,845 - 18,000) = ₹1,845$$

Therefore,

$$\text{Govind's gain} = ₹(1,845 - 1,800) = ₹45$$

10. Find the compound interest on ₹4,000 accrued in three years, when the rate of interest is 8% for the first year and 10% per year for the second and the third years.

Solution:

$$\text{Given: } P = ₹4,000; T = 3 \text{ years}$$

Interest for the 1st year, $R = 8\%$

$$\begin{aligned} I &= (P \times R \times T)/100 \\ &= (4000 \times 8 \times 1)/100 \\ &= ₹320 \end{aligned}$$

And,

$$\begin{aligned} \text{Amount after the 1st year} &= ₹(4,000 + 320) \\ &= ₹4,320 \end{aligned}$$

Now,

Interest for the 2nd year, $R = 10\%$ and $P = ₹4,320$

$$\begin{aligned} I &= (P \times R \times T)/100 \\ &= (4320 \times 10 \times 1)/100 \\ &= ₹432 \end{aligned}$$

And,

$$\begin{aligned} \text{Amount after the 2nd year} &= ₹(432 + 4,320) \\ &= ₹4,752 \end{aligned}$$

Next,

Interest for the 3rd year, $R = 10\%$ and $P = ₹4,752$

$$\begin{aligned} I &= (P \times R \times T)/100 \\ &= (4,752 \times 10 \times 1)/100 \\ &= ₹475.20 \end{aligned}$$

And,

$$\begin{aligned} \text{Amount after the 3rd year} &= ₹(475.20 + 4,752) \\ &= ₹5,227.20 \end{aligned}$$

Hence,

$$\begin{aligned} \text{The compound interest} &= ₹(5227.20 - 4,000) \\ &= ₹1,227.20 \end{aligned}$$