

Exercise 5(B)

Factorize:

1. $a^2 + 10a + 24$

Solution:

We have, $a^2 + 10a + 24$
By splitting the middle term, we get
 $= a^2 + 6a + 4a + 24$
 $= a(a + 6) + 4(a + 6)$
 $= (a + 4)(a + 6)$

2. $a^2 - 3a - 40$

Solution:

We have, $a^2 - 3a - 40$
By splitting the middle term, we get
 $= a^2 - 8a + 5a - 40$
 $= a(a - 8) + 5(a - 8)$
 $= (a + 5)(a - 8)$

3. $1 - 2a - 3a^2$

Solution:

We have, $1 - 2a - 3a^2$
By splitting the middle term, we get
 $= 1 - 3a + a - 3a^2$
 $= 1(1 - 3a) + a(1 - 3a)$
 $= (1 + a)(1 - 3a)$

4. $x^2 - 3ax - 88a^2$

Solution:

We have, $x^2 - 3ax - 88a^2$
By splitting the middle term, we get
 $= x^2 - 11ax + 8ax - 88a^2$
 $= x(x - 11a) + 8a(x - 11a)$
 $= (x + 8a)(x - 11a)$

5. $6a^2 - a - 15$

Solution:

We have, $6a^2 - a - 15$
By splitting the middle term, we get
 $= 6a^2 + 9a - 10a - 15$
 $= 3a(2a + 3) - 5(2a + 3)$
 $= (3a - 5)(2a + 3)$

6. $24a^3 + 37a^2 - 5a$

Solution:

We have, $24a^3 + 37a^2 - 5a$

Taking 'a' common from all

$$= a (24a^2 + 37a - 5)$$

$$= a (24a^2 + 40a - 3a - 5) \quad \{\text{By splitting the middle term}\}$$

$$= a [8a(3a + 5) - 1(3a + 5)]$$

$$= a [(8a - 1) (3a + 5)]$$

$$= a (8a - 1) (3a + 5)$$

7. $a(3a - 2) - 1$

Solution:

We have, $a(3a - 2) - 1$

On expanding,

$$= 3a^2 - 2a - 1$$

By splitting the middle term, we get

$$= 3a^2 - 3a + a - 1$$

$$= 3a(a - 1) + 1(a - 1)$$

$$= (3a + 1) (a - 1)$$

8. $a^2b^2 + 8ab - 9$

Solution:

We have, $a^2b^2 + 8ab - 9$

By splitting the middle term, we get

$$= a^2b^2 + 9ab - ab - 9$$

$$= ab(ab + 9) - 1(ab + 9)$$

$$= (ab - 1) (ab + 9)$$

9. $3 - a(4 + 7a)$

Solution:

We have, $3 - a(4 + 7a)$

On expanding,

$$= 3 - 4a - 7a^2$$

By splitting the middle term, we get

$$= 3 + 3a - 7a - 7a^2$$

$$= 3(1 + a) - 7a(1 + a)$$

$$= (1 + a) (3 - 7a)$$

10. $(2a + b)^2 - 6a - 3b - 4$

Solution:

We have, $(2a + b)^2 - 6a - 3b - 4$

$$= (2a + b)^2 - 3(2a + b) - 4$$

Let's assume that $(2a + b) = x$

So, the expression becomes

$$= x^2 - 3x - 4$$

By splitting the middle term, we get

$$= x^2 - 4x + x - 4$$

$$= x(x - 4) + 1(x - 4)$$

$$= (x - 4)(x + 1)$$

Resubstituting the value of x , we get

$$= (2a + b - 4)(2a + b + 1)$$

11. $1 - 2(a + b) - 3(a + b)^2$

Solution:

We have, $1 - 2(a + b) - 3(a + b)^2$

Let's assume $(a + b) = x$

Then, the expression becomes

$$= 1 - 2x - 3x^2$$

By splitting the middle term, we get

$$= 1 - 3x + x - 3x^2$$

$$= 1(1 - 3x) + x(1 - 3x)$$

$$= (1 - 3x)(1 + x)$$

Resubstituting the value of x , we get

$$= [1 - 3(a + b)][1 + (a + b)]$$

$$= (1 - 3a - 3b)(1 + a + b)$$

12. $3a^2 - 1 - 2a$

Solution:

We have, $3a^2 - 1 - 2a$

Rearranging,

$$= 3a^2 - 2a - 1$$

By splitting the middle term, we get

$$= 3a^2 - 3a + a - 1$$

$$= 3a(a - 1) + 1(a - 1)$$

$$= (3a + 1)(a - 1)$$

13. $x^2 + 3x + 2 + ax + 2a$

Solution:

We have, $x^2 + 3x + 2 + ax + 2a$

By splitting the middle term, we get

$$= (x^2 + 2x + x + 2) + ax + 2a$$

$$= x(x + 2) + 1(x + 2) + a(x + 2)$$

$$= (x + 2)(x + a + 1)$$

14. $(3x - 2y)^2 + 3(3x - 2y) - 10$

Solution:

We know, $(3x - 2y)^2 + 3(3x - 2y) - 10$

Let's assume that $(3x - 2y) = a$

So, the expression becomes

$$= a^2 + 3a - 10$$

By splitting the middle term, we get

$$= a^2 + 5a - 2a - 10$$

$$= a(a + 5) - 2(a + 5)$$

$$= (a - 2)(a + 5)$$

$$= (3x - 2y + 5)(3x - 2y - 2)$$

15. $5 - (3a^2 - 2a)(6 - 3a^2 + 2a)$

Solution:

Given, $5 - (3a^2 - 2a)(6 - 3a^2 + 2a)$

$$= 5 - (3a^2 - 2a)[6 - (3a^2 - 2a)]$$

Let's substitute $(3a^2 - 2a) = x$

And, the expression becomes,

$$= 5 - x(6 - x)$$

$$= 5 - 6x + x^2$$

$$= 5 - 5x - x + x^2$$

$$= 5(1 - x) - x(1 - x)$$

$$= (1 - x)(5 - x)$$

$$= (x - 1)(x - 5)$$

$$= (3a^2 - 2a - 1)(3a^2 - 2a - 5)$$

Now,

$$= (3a^2 - 3a + a - 1)(3a^2 + 3a - 5a - 5) \quad \{\text{By splitting the middle term}\}$$

$$= [3a(a - 1) + 1(a - 1)][3a(a + 1) - 5(a + 1)]$$

$$= [(3a + 1)(a - 1)][(3a - 5)(a + 1)]$$

$$= (3a + 1)(3a - 5)(a + 1)(a - 1)$$

16. $1/35 + 12a/35 + a^2$

Solution:

We have, $1/35 + 12a/35 + a^2$

Taking common,

$$= 1/35 (1 + 12a + 35a^2)$$

$$= 1/35 (35a^2 + 12a + 1)$$

$$= 1/35 (35a^2 + 7a + 5a + 1) \quad \{\text{By splitting the middle term}\}$$

$$= 1/35 [7a(5a + 1) + 1(5a + 1)]$$

$$= 1/35 [(7a + 1)(5a + 1)]$$

$$= [(7a + 1)(5a + 1)] / 35$$

17. $(x^2 - 3x)(x^2 - 3x - 1) - 20$.

Solution:

We have, $(x^2 - 3x)(x^2 - 3x - 1) - 20$
 $= (x^2 - 3x)[(x^2 - 3x) - 1] - 20$

Let's

$$= a[a - 1] - 20 \dots (\text{Taking } x^2 - 3x = a)$$

$$= a^2 - a - 20$$

$$= a^2 - 5a + 4a - 20$$

$$= a(a - 5) + 4(a - 5)$$

$$= (a - 5)(a + 4)$$

$$= (x^2 - 3x - 5)(x^2 - 3x + 4)$$

18. Find each trinomial (quadratic expression), given below, find whether it is factorisable or not. Factorise, if possible.

(i) $x^2 - 3x - 54$

(ii) $2x^2 - 7x - 15$

(iii) $2x^2 + 2x - 75$

(iv) $3x^2 + 4x - 10$

(v) $x(2x - 1) - 1$

Solution:

(i) Given, $x^2 - 3x - 54$

On comparing with the general form $ax^2 + bx + c$, we get

$$a = 1, b = -3 \text{ and } c = -54$$

$$\text{So, } b^2 - 4ac = (-3)^2 - 4(1)(-54) = 9 + 216 = 225$$

225 is a perfect square

Thus, $x^2 - 3x - 54$ is factorisable

Now,

$$\begin{aligned} x^2 - 3x - 54 &= x^2 - 9x + 6x - 54 \\ &= x(x - 9) + 6(x - 9) \\ &= (x + 6)(x - 9) \end{aligned}$$

(ii) Given, $2x^2 - 7x - 15$

On comparing with the general form $ax^2 + bx + c$, we get

$$a = 2, b = -7 \text{ and } c = -15$$

$$\text{So, } b^2 - 4ac = (-7)^2 - 4(2)(-15) = 49 + 120 = 169$$

169 is a perfect square

Thus, $2x^2 - 7x - 15$ is factorisable

Now,

$$\begin{aligned} 2x^2 - 7x - 15 &= 2x^2 - 10x + 3x - 15 \\ &= 2x(x - 5) + 3(x - 5) \\ &= (2x + 3)(x - 5) \end{aligned}$$

(iii) Given, $2x^2 + 2x - 75$

On comparing with the general form $ax^2 + bx + c$, we get

$$a = 2, b = 2 \text{ and } c = -75$$

$$\text{So, } b^2 - 4ac = (2)^2 - 4(2)(-75) = 4 + 600 = 604$$

604 is not a perfect square

Thus, $2x^2 + 2x - 75$ is not factorizable

(iv) Given, $3x^2 + 4x - 10$

On comparing with the general form $ax^2 + bx + c$, we get

$$a = 3, b = 4 \text{ and } c = -10$$

$$\text{So, } b^2 - 4ac = (4)^2 - 4(3)(-10) = 16 + 120 = 136$$

136 is not a perfect square

Thus, $3x^2 + 4x - 10$ is not factorizable

(v) Given, $x(2x - 1) - 1$

$$= 2x^2 - x - 1$$

On comparing with the general form $ax^2 + bx + c$, we get

$$a = 2, b = -1 \text{ and } c = -1$$

$$\text{So, } b^2 - 4ac = (-1)^2 - 4(2)(-1) = 1 + 8 = 9$$

9 is a perfect square

Thus, $x(2x - 1) - 1$ is factorisable

Now,

$$\begin{aligned} x(2x - 1) - 1 &= 2x^2 - x - 1 \\ &= 2x^2 - 2x + x - 1 \\ &= 2x(x - 1) + 1(x - 1) \\ &= (2x + 1)(x - 1) \end{aligned}$$

Myclass24
Your Class. Your Pace.

19. Factorise:

(i) $4\sqrt{3}x^2 + 5x - 2\sqrt{3}$

(ii) $7\sqrt{2}x^2 - 10x - 4\sqrt{2}$

Solution:

(i) We have, $4\sqrt{3}x^2 + 5x - 2\sqrt{3}$

By splitting the middle term, we get

$$= 4\sqrt{3}x^2 + 8x - 3x - 2\sqrt{3}$$

$$= 4x(\sqrt{3}x + 2) - \sqrt{3}(\sqrt{3}x + 2)$$

$$= (4x - \sqrt{3})(\sqrt{3}x + 2)$$

(ii) We have, $7\sqrt{2}x^2 - 10x - 4\sqrt{2}$

By splitting the middle term, we get

$$= 7\sqrt{2}x^2 - 14x + 4x - 4\sqrt{2}$$

$$= 7\sqrt{2}x(x - \sqrt{2}) + 4(x - \sqrt{2})$$

$$= (7\sqrt{2}x + 4)(x - \sqrt{2})$$

20. Give possible expressions for the length and the breadth of the rectangle whose area is $12x^2 - 35x + 25$.

Solution:

We have, $12x^2 - 35x + 25$

By splitting the middle term, we get

$$= 12x^2 - 20x - 15x + 25$$

$$= 4x(3x - 5) - 5(3x - 5)$$

$$= (3x - 5)(4x - 5)$$

Hence,

Length = $(3x - 5)$ and breadth = $(4x - 5)$ or,

Length = $(4x - 5)$ and breadth = $(3x - 5)$



Myclass24
Your Class. Your Pace.