

Chapter 3 -Compound Interest

Exercise 3(D)

1. The cost of a machine is supposed to depreciate each year at 12% of its value at the beginning of the year. If the machine is valued at ₹44,000 at the beginning of 2008, find its value:

(i) at the end of 2009.

(ii) at the beginning of 2007.

Solution:

Given:

Cost of machine in 2008 (P) = ₹44,000 and its depreciation rate = 12%

Then,

(i) The cost of machine at the end of 2009 will be

$$= P(1 - r/100)^n$$

$$= 44000 (1 - 12/100)^2$$

$$= 44000 (88/100)^2$$

$$= 34073.60$$

Hence, the cost of the machine at the end of 2009 is ₹34,073.60

(ii) The cost of machine at the beginning of 2007(P)

$$A = P(1 - r/100)^n$$

$$44000 = P(1 - 12/100)^2$$

$$44000 = P(88/100)^2$$

$$P = \frac{44000 \times 100^2}{88^2}$$

$$= 50000$$

Hence, the cost of the machine at the beginning of 2007 is ₹50,000

2. The value of an article decreases for two years at the rate of 10% per year and then in the third year it increases by 10%. Find the original value of the article, if its value at the end of 3 years is ₹40,095.

Solution:

Let's assume x to be the value of the article

Given, the value of an article decreases for two years at the rate of 10% per year.

So,

The value of the article at the end of the 1st year will be

$$x - 10\% \text{ of } x = x - 0.10x = 0.90x$$

And,

The value of the article at the end of the 2nd year will be

$$0.90x - 10\% \text{ of } (0.90x) = 0.90x - 0.09x = 0.81x$$

Now,

The value of the article increases in the 3rd year by 10%.

So, the value of the article at the end of 3rd year will be

$$0.81x + 10\% \text{ of } (0.81x) = 0.81x + 0.081x = 0.891x$$

Given that, the value of the article at the end of 3 years is ₹40,095

Then,

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$$\begin{aligned}0.891x &= 40095 \\x &= 40095/0.891 \\&= 45000\end{aligned}$$

Therefore,
The original value of the article is ₹45,000.

3, According to a census taken towards the end of the year 2009, the population of a rural town was found to be 64,000. The census authority also found that the population of this particular town had a growth of 5% per annum. In how many years after 2009 did the population of this town reach 74,088?

Solution:

Given: Population in 2009 (P) = 64,000

Let's assume that after 'n' years its population to be 74,088 (A)

Also, given

Growth rate = 5% per annum

We know that,

$$A = P(1 + r/100)^n$$

$$74088 =$$

$$74088 =$$

$$9261$$

$$(21/$$

$$\text{On}$$

$$n =$$

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Therefore, 2009 for the population of the town to reach 74,088

4. The population of a town decreased by 12% during 1998 and then increased by 8% during 1999. Find the population of the town, at the beginning of 1998, if at the end of 1999 its population was 2,85,120.

Solution:

Let's assume the population in the beginning of 1998 be P

Given, the population at the end of 1999 = 2,85,120 (A)

According to the question,

$$r_1 = -12\% \text{ and } r_2 = +8\%$$

Then,

$$A = P(1 - r_1/100) (1 + r_2/100)$$

$$285120 = P(1 - 12/100) (1 + 8/100)$$

$$285120 = P(22/25) (27/25)$$

$$P = (285120 \times 25 \times 25)/(22 \times 27)$$

$$= 300000$$

Therefore, the population of the town at the beginning of 1998 was 3,00,000

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$$\begin{aligned} \text{C.I.} &= P(1 + r/100)^n - P \\ &= 7500(1 + y/100)^2 - 7500 \end{aligned}$$

It's given that, C.I. - S.I. = ₹12

$$\begin{aligned} 7500(1 + y/100)^2 - 7500 - 150y &= 12 \\ 7500(1 + y^2/10000 + 2y/100) - 7500 - 150y &= 12 \\ 7500 + 75y^2/100 + 150y - 7500 - 150y &= 12 \\ 75y^2/100 &= 12 \\ 3y^2/4 &= 12 \\ y^2 &= (12 \times 4)/3 = 16 \\ y &= 4\% \end{aligned}$$

Hence, the rate of interest is 4%

7. A sum of money lent out at C.I. at a certain rate per annum becomes three times of itself in 10 years. Find in how many years will the money become twenty-seven times of itself at the same rate of interest p.a.

Solution:

Let's assume the sum to be ₹y and rate = r%

From the condition to 1st condition

Amount

We have

A =

3y =

3 =



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According to

Let's consider the amount in n years amount will be ₹27y

$$= P(1 + r/100)^n$$

$$27y = y(1 + r/100)^n$$

$$3^3 = (1 + r/100)^n$$

Using (1), we have

$$[(1 + r/100)^{10}]^3 = (1 + r/100)^n$$

$$(1 + r/100)^{30} = (1 + r/100)^n$$

On comparing,

$$n = 30$$

Hence, it will 30 years for the money to become 27 times of itself.

8. Mr. Sharma borrowed a certain sum of money at 10% per annum compounded annually. If by paying ₹19,360 at the end of the second year and ₹31,944 at the end of the third year he clears the debt; find the sum borrowed by him.

Solution:

Let's assume the sum which Sharma borrowed as P

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Given that the rate of interest is 10% and compounded annually

Now, according to the question

At the end of the two years the amount will

$$\begin{aligned}A_1 &= P(1 + r/100)^n \\ &= P(1 + 10/100)^2 \\ &= P(11/10)^2\end{aligned}$$

And,

Mr. Sharma paid ₹19,360 at the end of the second year.

So, for the third year the principal will be ($A_1 - ₹19,360$)

Also given, he cleared the debt by paying ₹31,944 at the end of the third year.

Now,

$$\begin{aligned}A_2 &= P(1 + r/100)^n \\ 31944 &= P[(1 + 10/100)^2 - 19360] (1 + 10/100)^1 \\ 29040 &= P[(11/10)^2 - 19360] \\ P(11/10)^2 &= 48400 \\ P &= 48400 \times (10/11)^2 \\ &= 40000\end{aligned}$$

Therefore, Mr. Sharma borrowed ₹40,000.

9. The compound interest for a year payable half-yearly and simple interest on a money lent out at 10% for a year is ₹15. Find the sum of money lent out.

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Let's assume the sum of money lent out to be ₹y

Calculating S.I.

$$\begin{aligned}\text{S.I.} &= (P \times r \times t) / 100 \\ &= (y \times 10 \times 1) / 100 \\ &= y/10\end{aligned}$$

And,

Calculating C.I.(compounded half-yearly)

$$\begin{aligned}\text{C.I.} &= P \{ [1 + r/(2 \times 100)]^{nx2} - 1 \} \\ &= y \{ [1 + 10/(2 \times 100)]^{1 \times 2} - 1 \} \\ &= y[(21/20)^2 - 1] \\ &= (41/400)y\end{aligned}$$

It's given that C.I. – S.I. = ₹15

So,

$$\begin{aligned}(41/400)y - y/10 &= 15 \\ y/400 &= 15 \\ y &= 6000\end{aligned}$$

Therefore, the sum of money lent out is ₹6,000

10. The ages of Pramod and Rohit are 16 years and 18 years respectively. In what ratio must they invest money at 5% p.a. compounded yearly so that both get the same sum on attaining the age of 25 years?

Solution:

Let's assume that ₹x and ₹y to be the money invested by Pramod and Rohit respectively such that they will get the same sum on attaining the age of 25 years.

Now,

Pramod will attain the age of 25 years after $(25 - 16) = 9$ years

Rohit will attain the age of 25 years after $(25 - 18) = 7$ years

So, we have

$$x(1 + 5/100)^9 = y(1 + 5/100)^7$$

$$x/y = 1/(1 + 5/100)^2$$

$$x/y = 400/441$$

Therefore,

Pramod and Rohit should invest in the ratio 400:441 respectively such that they will get the same sum on attaining the age of 25.



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