

EXERCISE 21C

1. Each face of a cube has perimeter equal to 32 cm. Find its surface area and its volume.

Solution:

Perimeter of a cube is

Perimeter = $4a$ where a is the length

It is given that perimeter of the face of the cube = 32 cm

$$4a = 32 \text{ cm}$$

$$a = 32/4$$

$$a = 8 \text{ cm}$$

Surface area of a cube with side ' a ' = $6a^2$

$$\text{So the surface area} = 6 \times 8^2 = 6 \times 64 = 384 \text{ cm}^2$$

Volume of a cube with side ' a ' = a^3

$$\text{So the volume} = 8^3 = 512 \text{ cm}^3$$

2. A school auditorium is 40 m long, 30 m broad and 12 m high. If each student requires 1.2 m^2 of the floor area; find the maximum number of students that can be accommodated in this auditorium. Also, find the volume of air available in the auditorium, for each student.

Solution:

It is given that

$$\text{Dimensions of the auditorium} = 40 \text{ m} \times 30 \text{ m} \times 12 \text{ m}$$

$$\text{Area of the floor} = 40 \times 30$$

It is given that each student requires 1.2 m^2 of the floor area

$$\text{Maximum number of students} = (40 \times 30) / 1.2 = 1000$$

Volume of the auditorium

$$= 40 \times 30 \times 12 \text{ m}^3$$

$$= \text{Volume of air available for 1000 students}$$

$$\text{Air available for each student} = (40 \times 30 \times 12) / 1000 = 14.4 \text{ m}^3$$

3. The internal dimensions of a rectangular box are $12 \text{ cm} \times x \text{ cm} \times 9 \text{ cm}$. If the length of the longest rod that can be placed in this box is 17 cm; find x .

Solution:

We know that

Length of longest rod = Length of the diagonal of the box

$$17 = \sqrt{12^2 + x^2 + 9^2}$$

By squaring on both sides

$$17^2 = 12^2 + x^2 + 9^2$$

$$x^2 = 17^2 - 12^2 - 9^2$$

$$x^2 = 289 - 144 - 81$$

$$x^2 = 64$$

$$x = 8 \text{ cm}$$

4. The internal length, breadth and height of a box are 30 cm, 24 cm and 15 cm. Find the largest number of cubes which can be placed inside this box if the edge of each cube is

(i) 3 cm

(ii) 4 cm

(iii) 5 cm

Solution:

(i) Number of cubes which can be placed along length = $30/3 = 10$

Number of cubes along the breadth = $24/3 = 8$

Number of cubes along the height = $15/3 = 5$

So the total number of cubes placed = $10 \times 8 \times 5 = 400$

(ii) Number of cubes which can be placed along length = $30/4 = 7.5$ (Take 7)

Number of cubes along the width = $24/4 = 6$

Number of cubes along the height = $15/4 = 3.75$ (Take 3)

So the total number of cubes placed = $7 \times 6 \times 3 = 126$

(iii) Number of cubes which can be placed along length = $30/5 = 6$

Number of cubes along the width = $24/5 = 4.5$ (Take 4)

Number of cubes along the height = $15/5 = 3$

So the total number of cubes placed = $6 \times 4 \times 3 = 72$

5. A rectangular field is 112 m long and 62 m broad. A cubical tank of edge 6 m is dug at each of the four corners of the field and the earth so removed is evenly spread on the remaining field. Find the rise in level.

Solution:

It is given that

Volume of the tank = Volume of the earth spread

$$4 \times 6^3 \text{ m}^3 = (112 \times 62 - 4 \times 6^2) \text{ m}^2 \times \text{Rise in level}$$

We know that

$$\text{Rise in level} = \frac{4 \times 6^3}{112 \times 62 - 4 \times 6^2}$$

$$= \frac{864}{6800}$$

$$= 0.127 \text{ m}$$

$$= 12.7 \text{ cm}$$