

EXERCISE 12.2

Write True or False and justify your answer:

1. The area of a triangle with base 4 cm and height 6 cm is 24 cm^2 .

Solution:

False

Justification:

$$\begin{aligned}\text{Area of triangle} &= \frac{1}{2} \times \text{Base} \times \text{Altitude} \\ &= \frac{1}{2} \times 4 \times 6 \\ &= 12\text{cm}^2\end{aligned}$$

Hence, the statement “the area of a triangle with base 4 cm and height 6 cm is 24 cm^2 ” is False.

2. The area of $\triangle ABC$ is 8 cm^2 in which $AB = AC = 4 \text{ cm}$ and $\angle A = 90^\circ$.

Solution:

True

Justification:

$$\begin{aligned}\text{Area of triangle} &= \frac{1}{2} \times \text{Base} \times \text{Altitude} \\ &= \frac{1}{2} \times 4 \times 4 \\ &= 8\text{cm}^2\end{aligned}$$

Hence, the statement is “area of $\triangle ABC$ is 8 cm^2 in which $AB = AC = 4 \text{ cm}$ and $\angle A = 90^\circ$ ” is True.

3. The area of the isosceles triangle is $\frac{5}{4}\sqrt{11}\text{cm}^2$, if the perimeter is 11 cm and the base is 5 cm.

Solution:

True

Justification:

According to the question,

$$\text{Perimeter} = 11\text{cm}$$

$$\text{And base, } a = 5$$

As the triangle is isosceles, $b = c$

$$\text{Perimeter} = 11$$

$$\Rightarrow a + b + c = 11$$

$$\Rightarrow 5 + b + b = 11$$

$$\Rightarrow 5 + 2b = 11$$

$$\Rightarrow 2b = 6$$

$$\Rightarrow b = 3$$

So, we have,

$$a = 5, b = 3, c = 3$$

$$s = (a + b + c)/2$$

$$\Rightarrow s = (5 + 3 + 3)/2 = 11/2$$

$$\text{Area of triangle} = \sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{\frac{11}{2} \left(\frac{11}{2} - 5 \right) \left(\frac{11}{2} - 3 \right) \left(\frac{11}{2} - 3 \right)}$$

$$= \sqrt{\frac{11}{2} \left(\frac{1}{2} \right) \left(\frac{5}{2} \right) \left(\frac{5}{2} \right)}$$

$$\Rightarrow \text{Area of triangle} = (5\sqrt{11})/4 \text{ cm}^2$$

Hence, the statement "The area of the isosceles triangle is $5/4 \sqrt{11} \text{ cm}^2$, if the perimeter is 11 cm and the base is 5 cm" is True.

4. The area of the equilateral triangle is $20\sqrt{3} \text{ cm}^2$ whose each side is 8 cm.

Solution:

False

Justification:

Area of an equilateral triangle of side $a = \sqrt{3}/4 a^2$

According to the question,

Area of a triangle = $20\sqrt{3} \text{ cm}^2$

$$\Rightarrow \sqrt{3}/4 a^2 = 20\sqrt{3}$$

$$\Rightarrow a^2 = 20 \times 4$$

$$\Rightarrow a^2 = 80$$

$$\Rightarrow a = 4\sqrt{5} \text{ cm}$$

Hence, the statement "the area of the equilateral triangle is $20\sqrt{3} \text{ cm}^2$ whose each side is 8 cm" is False.

